

1 On the potential for GWAS with phenotypic 2 population means and allele-frequency data 3 (popGWAS)

4
5 Markus Pfenninger^{1,2,3*}

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7 ¹ Dept. Molecular Ecology, Senckenberg Biodiversity and Climate Research Centre, Georg-Voigt-Str. 14-16,
8 D-60325 - Frankfurt am Main, Germany

9 ² LOEWE Centre for Translational Biodiversity Genomics, Senckenberg Biodiversity and Climate Research
10 Centre, Senckenberganlage 25, D-60325 - Frankfurt am Main, Germany

11 ³ Institute for Molecular and Organismic Evolution, Johannes Gutenberg University, Johann-Joachim-
12 Becher-Weg 7, D-55128 - Mainz, Germany

13

14 *Corresponding author

15 Correspondence: Markus.Pfenninger@senckenberg.de

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18 **ABSTRACT**

19 It is vital to understand the genomic basis of differences in ecologically important traits
20 if we are to understand the impact of global change on biodiversity and enhance our
21 ability for targeted intervention. This study explores the potential of a novel genome-
22 wide association study (GWAS) approach for identifying loci underlying quantitative
23 polygenic traits in natural populations, based on phenotypic population means and
24 genome-wide allele frequency data as obtained e.g. by PoolSeq approaches. Extensive
25 population genetic forward simulations demonstrate that the approach is generally
26 effective for oligogenic and moderately polygenic traits and relatively insensitive to low
27 heritability. However, applicability is limited for highly polygenic architectures and
28 pronounced population structure. The required sample size is moderate with very good
29 results being obtained already for a few dozen populations scored. When combined
30 with machine learning for feature selection, the method performs very well in
31 predicting population means. The data efficiency of the method, particularly when using
32 pooled sequencing and bulk phenotyping, makes GWAS studies more accessible for
33 research in biodiversity genomics. Moreover, in a direct comparison to individual based
34 GWAS, the proposed method performed consistently better with regard to the number
35 of true positive loci identified and prediction accuracy. Overall, this study highlights the
36 promise of popGWAS for dissecting the genetic basis of complex traits in natural
37 populations.

38 **Keywords:** biodiversity population genomics, molecular trait basis

39

Introduction

41 A major goal as well as a major challenge in evolutionary biology is to understand how genes
42 influence traits, i.e. the genotype-phenotype link, (Brandes et al., 2022; Uffelmann et al., 2021).
43 The difficulties in achieving this goal are primarily due to the fact that the heritable variation of
44 many, if not most, relevant phenotypes is determined by small contributions from many genetic
45 loci (Sella & Barton, 2019). Such complex traits are usually influenced by a few dozen genes that
46 are mechanistically directly involved in their expression, but often also by numerous, if not
47 almost all, other genes as well as the environment in the widest sense (Boyle et al., 2017).

48 Genome-wide association studies (GWAS) are commonly used to link complex phenotypic
49 traits to their genomic basis (Brandes et al., 2022; Visscher et al., 2012). However, given the
50 complexity of causal mechanisms and the small effects of individual loci, often only a small
51 fraction of the genetic variation underlying phenotypic variance is identified, despite the
52 considerable logistic effort in terms of the number of phenotyped and genotyped individuals
53 (Brandes et al., 2022; Visscher et al., 2017). As a result, accurate predictions of phenotypes from
54 genomic data are still quite limited and there is currently no other strategy than to keep
55 increasing sample sizes (Brandes et al., 2022). This is a problem in the medical sciences
56 (Shendure et al., 2019), but the greater challenge for science and society probably lies in
57 addressing the global biodiversity crisis. It would be highly desirable to have affordable methods
58 to accurately understand the genomic basis of relevant traits and predict (non-model) species
59 responses to all aspects of global change (Bernatchez et al., 2023; Waldvogel et al., 2020).

60 GWAS with wild populations has been advocated for some time (Santure & Garant, 2018).
61 However, despite recent progress in high throughput, automated phenotyping (Dunker et al.,
62 2022; Tills et al., 2023; Xie & Yang, 2020), the advances of biodiversity genomics in obtaining
63 high quality reference genomes for almost every species (Exposito-Alonso et al., 2020; Formenti
64 et al., 2022) and the possibility to gain cost-effective genome-wide population data (Czech,
65 Peng, Spence, Lang, Bellagio, Hildebrandt, Fritschi, Schwab, Rowan, & Weigel, 2022; Schlötterer
66 et al., 2014), relatively few empirical studies are currently available [missing citations]. This gap between
67 the possibilities and actual practical application in biodiversity conservation (Heuertz et al.,
68 2023; Hogg, 2023) is probably as much due to the still existing logistic and financial challenges as
69 to a lack of data- and resource-efficient methods.

70 Here, I explore the potential of a new GWAS approach using phenotypic population means
71 and genome-wide allele-frequency data. The rationale behind the approach is straightforward.
72 If a quantitative polygenic trait has an additive genetic component, an individual's phenotypic
73 trait value should at least roughly correlate with the number of trait-increasing alleles at the
74 underlying loci (Uffelmann et al., 2021). Consequently, it was theoretically expected (Orr, 1998;
75 Pritchard & Di Rienzo, 2010) and empirically shown (Turchin et al., 2012) that trait-increasing
76 alleles will tend to have greater frequencies in the population with higher mean trait values,
77 compared to the population with a lower trait mean. When examining populations with a range
78 of different phenotypic trait means, we may therefore expect that the allele frequencies at the
79 trait-affecting loci show a linear or at least steady relation with the observed trait means
80 (Barton, 1999). I hypothesise here that this predicted relation can be exploited to distinguish
81 potentially causal loci (and the linked variation) from loci not associated with the focal trait. In
82 case of a successful evaluation, the major advantages of the proposed approach would be the
83 reduced sequencing effort by the possibility to use pooled population samples (PoolSeq) and

84 the opportunity to use bulk phenotyping (e.g. by satellite imaging, flow-cytometry, etc.) on
85 traits for which individual phenotyping is difficult or tedious.

86 The most important assumption for the approach is obviously that observed population
87 differences in the focal trait means have at least partially a genetic basis. Since the environment
88 has usually an effect on the phenotype (Sella & Barton, 2019), total phenotypic variance should
89 be adjusted for known fixed environmental effects, because this increases the fraction of
90 variance due to genetic factors (Visscher et al. 2008). Predicting additive genetic values with
91 even higher accuracy can be achieved by taking into account GxE interactions through repeated
92 phenotypic measurements of the same individuals under different environmental conditions,
93 e.g. by time series (Visscher et al. 2008). I assumed therefore that environmental influence on
94 the phenotypic trait variance among populations has been statistically removed as much as
95 possible (Harpak & Przeworski, 2021). Similarly important is the assumption that the genetic
96 variance of the focal quantitative trait can be adequately described by an additive model. Both
97 empirical and theoretical evidence suggests that this is indeed the case for most complex traits
98 (Hill et al., 2008). Even though epistatic interactions are wide spread (Mackay, 2014), Sella and
99 Barton (Sella & Barton, 2019) argue that the marginal allelic effects on quantitative traits are
100 well approximated by a simple additive model.

101 The aims of this study were i) to understand whether and under which circumstances
102 the hypothesised pattern of a linear relation between the population allele frequencies at
103 causal loci and the phenotypic population means of the respective trait emerges, ii) to
104 evaluate the influence of population genetic parameters of typical natural systems and the
105 experimental design on the likelihood of identifying causal loci underlying an additive
106 quantitative trait, in particular to elucidate the limits of the approach with regard to genetic
107 architecture and population structure, iii) to compare proposed method with the
108 performance of an individual-based GWAS, iv) to explore the possibilities for statistical
109 genomic prediction of phenotypic population means from the allele frequencies at
110 identified loci, and v) to evaluate the statistical power of the method for a realistic range of
111 effective genome sizes. I used individual-based population genomic forward simulations
112 and machine learning approaches (minimum entropy feature selection) for prediction and
113 utilised an information theory-based framework for evaluation of the proposed method.

114 Material and methods

115 Rationale of the method

116 *Expectation of a positive correlation between quantitative trait loci allele frequencies and* 117 *phenotypic population means.*

118 Consider a biallelic, codominant system for the additively heritable component of a
119 quantitative trait with n loci contributing to the trait. In this system, all loci contribute
120 equally to the phenotypic trait, with one allele per locus making a greater contribution than
121 the other. The phenotypic trait value x of an individual can then be determined by simply
122 adding up the number of trait-increasing alleles (g with values of 0, 1 or 2) over all n
123 quantitative trait loci (QTL) and multiplying this sum with a scaling constant k

$$124 \quad (1) \quad x = k \times (g_1 + g_2 + \dots + g_n)$$

125 When adding more individuals, the phenotypic population trait mean is defined as the
126 mean of the row sums:

$$\begin{array}{rccccc}
 & & QTL_1 & \cdots & \cdots & QTL_n & & \text{individual trait value} \\
 & Ind_1 & g_{11} & g_{12} & \cdots & g_n & & x_1 = k \times \sum_{l=1}^n g_{1l} \\
 & Ind_2 & g_{21} & \cdots & \cdots & \cdots & & \cdots \\
 127 & (2) & \cdots & \cdots & \cdots & \cdots & & \cdots \\
 & Ind_m & g_{m1} & \cdots & \cdots & g_{mn} & & x_m = k \times \sum_{l=1}^n g_{ml} \\
 & & & & & & & \text{population trait mean} \\
 & & & & & & & \bar{x} = \frac{\sum_{i=1}^m x_i}{m}
 \end{array}$$

128 The columns of this matrix can be used to calculate the population allele frequency (AF)
 129 of the trait increasing allele for each QTL.

$$\begin{array}{rccccc}
 & & QTL_1 & \cdots & \cdots & QTL_n & & \text{individual trait value} \\
 & Ind_1 & g_{11} & g_{12} & \cdots & g_n & & x_1 = k \times \sum_{l=1}^n g_{1l} \\
 & Ind_2 & g_{21} & \cdots & \cdots & \cdots & & \cdots \\
 130 & (3) & \cdots & \cdots & \cdots & \cdots & & \cdots \\
 & Ind_m & g_{m1} & \cdots & \cdots & g_{mn} & & x_m = k \times \sum_{l=1}^n g_{ml} \\
 & & & & & & & \text{population trait mean} \\
 & AF & AF_1 = \frac{\sum_{i=1}^m g_i}{2m} & \cdots & \cdots & AF_1 = \frac{\sum_{i=1}^m g_i}{2m} & \text{mean QTL AF} & \bar{AF} = \frac{\sum_{i=1}^n AF_i}{n} \sim \bar{x} = \frac{\sum_{i=1}^m x_i}{m}
 \end{array}$$

131 The mean population allele frequency at the QTL loci is thus directly proportional to the
 132 phenotypic population trait mean. This relationship remains unchanged even if the
 133 individual locus contributions are not identical, with some loci contributing more or less to
 134 the phenotypic trait value. In this case, a scaling vector is required to weigh the individual
 135 locus contributions to individual trait values, and those of the AFs to the population trait
 136 mean. Since the AFs are by definition bounded by zero and one, the population trait mean is
 137 minimal when the allele frequencies of the trait-increasing allele at all QTL are zero and
 138 maximal when all QTL AFs are one. This proportionality links the individual genotypes and
 139 the AFs at the QTL linearly with the population trait mean.

140 If we extend this to a set of populations and order them with decreasing phenotypic
 141 population means, we can be sure that the mean QTL AFs of the populations will also be
 142 ordered in decreasing sequence:

$$\begin{array}{rccccc}
 & & Pop_1 & Pop_2 & \cdots & Pop_n \\
 & \text{population trait mean} & \bar{x}_1 > & \bar{x}_2 > & \cdots & \bar{x}_n \\
 & & \sim & \sim & \cdots & \sim \\
 143 & (4) & \text{mean QTL AF} & \bar{AF}_1 > & \bar{AF}_2 > & \cdots & \bar{AF}_n \\
 & & QTL_1 & AF_{11} & AF_{21} & \cdots & AF_{11} \\
 & & QTL_2 & AF_{12} & AF_{22} & \cdots & \cdots \\
 & & \cdots & \cdots & \cdots & \cdots & \cdots \\
 & & QTL_m & AF_{1m} & \cdots & \cdots & AF_{nm}
 \end{array}$$

144 The answer to whether the allele frequencies in every row i.e. at every contributing
 145 locus can be used to predict the population trait mean depends on whether the expected
 146 covariance between these two vectors is positive:

$$147 \quad (5) \quad E[\text{cov}(QTL_m, \text{population trait mean})] > 0$$

148 where

149 (6) $\text{cov}[\text{QTL}_m, \text{population trait mean}] = E[\sum_{i=1}^n (\text{AF}_{im} - E[\text{AF}_m]) * (\bar{x}_i - E[\bar{X}])]$

150 with \bar{X} representing the grand mean over all populations. As all elements in the QTL
151 matrix are positive, they inherently tend to contribute positively to their column means.
152 Therefore, AF larger than the overall AF mean at his locus tend to be on the left side of the
153 population closest to the overall phenotypic mean in the ordered matrix above. Conversely,
154 AF smaller than the locus AF mean are rather on the right. This leads intuitively to a
155 positive expected covariance between each row and the column mean, in particular if the
156 number of populations becomes large. Conversely, the AF at (unlinked) loci not
157 contributing to the phenotypic population trait mean have an expectation of zero.

158 *Testing the expectations of a detectable linear relation between allele frequencies and*
159 *phenotypic population means*

160 I tested these general expectations and the effect of different scaling vectors for the
161 effect size distribution of QTL with a first set of simulations. I generated a matrix of size $n \times$
162 m populated with random AF between zero and 1. To avoid stochastic effects due to sample
163 size, the number of populations n was fixed at 10,000. The number of QTL m was varied
164 from oligogenic to highly polygenic (10, 20, 50, 100, 200, 500, 1000, 2000, 5000). Three
165 different distributions of loci effects were tested, i) a flat distribution with all loci
166 contributing equally, ii) a mildly decreasing exponential function and iii) a steeply
167 decreasing exponential function with few loci contributing much and many very little
168 (Supplemental Figure 1).

169 Each of the m columns was used to calculate the phenotypic population mean of the
170 respective population by adding up the AF multiplied with the respective locus weight. The
171 resulting n phenotypic population means were then correlated to the n AF of each of the m
172 loci and the resulting m Pearson correlation coefficients (i.e. the standardized covariance)
173 recorded. From these, mean and standard deviation were calculated and tested, whether
174 they conform to a normal distribution (scipy.stats.normaltest). Furthermore, a second
175 matrix of identical size was populated with random AF, and the correlation of these non-
176 contributing loci to the population means derived from the QTL matrix was computed. The
177 simulations were repeated 10 times in every possible parameter combination and the
178 results averaged (Supplemental Script 1).

179 Individual based Wright-Fisher forward model used for simulation

180 A Wright-Fisher individual forward genetic simulation model was used to investigate the
181 potential of a genome-wide association study based on the means of a population trait and
182 population allele frequency data. As this model formed the basis for all further simulations,
183 its general structure is first described.

184 In the simulation, all loci were assumed to be unlinked, thus representing haplotypes in
185 LD rather than single SNPs. (Visscher et al., 2017). For each simulation run, the initial allele
186 frequencies for all loci in the total population were randomly drawn from a beta function
187 with parameters $\alpha = \beta = 0.5$ in a range 0.1 to 0.9. To generate a hermaphroditic and diploid
188 individual, two alleles were randomly drawn with a probability based on their frequency at
189 the respective locus, and the resulting genotype at this locus was recorded. This process
190 was repeated for all loci. As a result, each individual was represented by a vector of biallelic
191 genotypes ($AA = 0$, $Aa; aA = 1$, $aa = 2$). To model a quantitative, fully additive trait, a
192 variable number of loci were assigned as quantitative trait loci (QTL). In addition, a much
193 larger number of neutral loci was modelled.

194 *Genetic architecture of the quantitative trait*

195 The continuous trait value was measured in arbitrary units. The allele (A) at each QTL
196 had no effect on the individual's trait value, resulting in a completely homozygous A
197 individual at the QTL having a phenotypic trait value of 0. The alternative allele (a) added a
198 locus-specific value to the trait. Two distributional extremes have been considered for the
199 allelic effects on the trait value: i) a uniform distribution where each locus contributes 0.5
200 units to the trait. An individual that is completely homozygous for the alternative allele a
201 therefore had a trait value equal to the number of QTL, ii) an exponential distribution with
202 few loci having large effects and many having very small effects, scaled such that the
203 maximum possible trait value was also equal to the number of QTL (see Supplementary
204 Figure 2A). To model the effect of phenotyping errors, unaccounted environmental
205 influence, and/or the unspecific contribution of the genomic background to the trait, a
206 random value drawn from a Gaussian distribution with a mean of zero and selectable
207 standard deviation between 0.1 and 3 was added to the genetically determined phenotype
208 value of each individual. The phenotypic value of each individual's trait was determined by
209 summing the allelic effects of all genotypes at all QTL loci plus the random value and the
210 result recorded.

211 It was assumed that all trait variation was based on standing genetic variation.
212 Mutations were not considered because new or low frequency mutations do not
213 substantially influence phenotypic population means and their AFs. In addition, mutations
214 are rare and mutations affecting a particular functional trait even rarer. Therefore,
215 restricting the simulations to standing genetic variation seemed reasonable.

216 *Reproduction and selection*

217 Subpopulations in each run were created from the same initially drawn random allele
218 frequency array, mimicking a common descent. Due to sampling variance, the realised allele
219 frequencies and thus the mean subpopulation trait value differed from the initial
220 frequencies of the total (ancestral) population. A subpopulation always comprised 500
221 adult individuals.

222 For reproduction, two random individuals were chosen with replacement from the adult
223 population. The genotype of an offspring individual at a locus was determined by randomly
224 choosing one of the two alleles from each designated parent at this locus. Each parent
225 fostered n_{juv} offspring; therefore, $2 \times n_{\text{juv}}$ were produced in each mating. After
226 reproduction, the parental generation was discarded to prevent overlapping generations.
227 Each generation had $N/2$ matings, resulting in an offspring population of $N \times n_{\text{juv}}$
228 individuals. This assured that the genotypes in each subpopulation were in Hardy-
229 Weinberg equilibrium after the first generation.

230 Because the offspring population was much larger than **the** the size of the adult
231 population, it was necessary to reduce it. This was achieved by a combination of 'hard'
232 natural selection and random mortality. An individual's survival to the adult stage was
233 determined by the absolute deviation of its phenotypic trait value from a pre-specified
234 selective trait optimum for the respective subpopulation. This selective trait optimum for a
235 subpopulation was determined by adding a random value taken from a Gaussian
236 distribution with a mean of zero and a standard deviation of 2.5 to the initial population
237 mean. An individual's survival probability was determined by an exponential decline
238 function with strength s (the exponent of the function, see Supplementary Figure 2B).
239 Individuals were randomly selected one by one from the offspring population, the distance
240 of their phenotype to the selective optimum calculated and their survival probability

241 calculated. A respectively biased coin was then tossed to determine their fate. This process
242 was repeated until the adult population size was reached, and any remaining offspring
243 individuals were indiscriminately discarded. If the phenotypic mean of the subpopulation
244 was close to or at the selective optimum (see below), this process resulted in stabilising
245 selection. If the population was away from the optimum, rapid directed selection towards
246 the optimum was observed, depending on the strength of selection.

247 *Population structure*

248 For the assessment of the effect of population structure, each subpopulation received in
249 every generation a certain number of migrants randomly chosen from all other
250 subpopulations. Both drift and selection towards different trait optima led to variation in
251 population trait means among the subpopulations.

252 Based on the model described above, I considered scenarios where subpopulations with
253 quantitative phenotypic population differences in mean for the trait in question were
254 screened from a larger total population. Although the population trait mean differences in
255 the simulation of this scenario were created by drift and local adaptation, any other source
256 of heritable phenotypic population differentiation, such as maladaptation, introgression, or
257 e.g. in the case of managed species, human choice, may also be the non-exclusive reasons for
258 differentiation in population means. The range of phenotypic variation among the
259 subpopulations was not predetermined, but an emergent feature of the simulation
260 parameters.

261 After evolving the subpopulations for the desired number of generations, phenotypic
262 trait means, and genome-wide allele frequencies were recorded. While the phenotypic
263 means for each subpopulation was calculated over all individuals, the allele frequencies
264 were estimated in a PoolSeq (Kofler et al., 2011) like fashion from subsamples of 50
265 individuals. The range of phenotypic trait means of the population sample was recorded.
266 Trait heritability was determined in the last generation by regressing the phenotypic values
267 of the offspring against the mean of their respective parents (Lynch & Walsh, 1998). As
268 measure for population subdivision due to drift, F_{ST} among all subpopulations was
269 calculated from the variance of the true allele frequencies (Wright, 1949).

270 Simulated scenarios

271 *Influence of natural system and experimental design factors*

272 In a first set of simulations, I explored the influence of factors inherent to the natural
273 system and the experimental design on population GWAS performance (Table 1). As factors
274 of the natural system, I assumed characteristics that are beyond control of the researcher,
275 such as heritability of the trait and its genetic architecture (number of QTL, distribution of
276 allele trait contribution). While the degree of population differentiation and range of
277 phenotypic differentiation are also inherent to the organism studied, the choice of samples
278 may allow a certain control over these parameters. The number of subpopulations screened
279 is clearly a study design decision (Table 1).

280 Table 1. Simulation parameters, their abbreviations, values used in simulations, their
281 biological meaning and whether the parameter is a feature of the natural system
282 under scrutiny or under the control of the researcher.

Parameter	Abbreviation	Values in the simulation	Biological meaning	Degree of knowledge in natural systems/under the control of study design
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Number of subpopulations scored for phenotypic population means and genome wide allele frequencies	n_pop	12, 24 36, 48, 60	-	Full control
Number of quantitative trait loci contributing to the focal trait	n_qtl	30, 50, 70, 110, 500	Genetic architecture of the trait	<i>A priori</i> unknown
Distribution of allelic effects on the focal trait	allelic_contr	Flat, exponential	Genetic architecture of the trait	<i>A priori</i> unknown
Standard deviation of random phenotypic variation added to individuals	env-var	0.1, 1, 2, 3	Heritability of the trait	<i>A priori</i> unknown
Number of migrants received in each subpopulation per generation	mig	0, 5, 10, 50, 100	Population structure	Partial control

283 A genetic trait architecture of 30, 50, 70, 110 and 500 loci, flat and exponential allelic
 284 effect distributions, as well as **environmental variance** and **phenotypic plasticity coefficients** of 0.1, 1, 2 and 3 were
 285 applied (Table 1). Selection strength was fixed at 0.5 (Supplemental Figure 2B). The
 286 number of immigrants reaching and reproducing in each subpopulation in each generation
 287 was varied between 5, 10, 50 and 100 individuals. Simulations were run for 30 generations
 288 among 12, 24, 36, 48 and 60 subpopulations of 500 individuals each (Table 1). For this set
 289 of simulations, 1000 neutral loci and a fixed outlier threshold (upper 5% quantile, either 21
 290 or 22 outlier loci, respectively) were applied. Each possible parameter combination was run
 291 in five replicates, resulting in 4000 simulation runs.

292 The effect of each parameter on PPV was assessed with ANOVA over all simulations,
 293 grouped after the respective parameter classes. The relative influence of the number of
 294 populations, QTL loci, distribution of allelic contributions, trait heritability, phenotypic
 295 range and population subdivision on the proportion of **TPL** among the outlier loci was
 296 determined with a General Linearized Model (GLM). **not previously defined**

297 *Hierarchical population structure*

298 The effect of a hierarchical population structure on popGWAS performance was assessed
 299 with a restricted parameter set (Table 2). Two, three and four regions were simulated, each
 300 consisting of 12 subpopulations. While there was gene-flow among the populations within
 301 the regions as described above, no gene-flow among regions was simulated. The initial
 302 degree of differentiation among regions was determined by first drawing one set of random
 303 (beta distributed) allele frequencies as described above. To start each independent region
 304 with slightly, but not completely different allele frequencies, a random variate from a
 305 normal distribution with mean 0 and either 0.05, 0.1 or 0.2 as standard deviation was then
 306 added to each of the initially drawn allele frequencies (Table 2). The simulations were then
 307 run as described above. The hierarchical population structure was not explicitly taken into
 308 account in statistical analysis but performed as described above.

309 Table 2. Simulation parameters for hierarchical population structure, their
 310 abbreviations, values used in simulations, their biological meaning and whether the
 311 parameter is a feature of the natural system under scrutiny or under the control of
 312 the researcher.

Parameter	Abbreviation	Values in the simulation	Biological meaning	Degree of knowledge in natural systems/under the control of study design
Number of regions with 12 subpopulations each	n_reg	2,3,4	-	Partial control
Number of quantitative trait loci contributing to the focal	n_qtl	30, 70, 110	Genetic architecture of the trait	<i>A priori</i> unknown

trait				
Distribution of allelic effects on the focal trait	allelic_contr	Flat, exponential	Genetic architecture of the trait	<i>A priori</i> unknown
Standard deviation of random phenotypic variation added to individuals	env_var	2	Heritability of the trait	<i>A priori</i> unknown
Number of migrants received in each subpopulation per generation	mig	5, 50	Gene-flow	Partial control

313 *Population based GWAS (popGWAS)*

314 Assuming a linear relation between the phenotypic (sub)population means, and the
315 population allele frequencies of the causal loci on the other, I calculated an ordinary linear
316 regression between these two variables for all loci in the genome for each simulation. I used
317 the resulting $-\log_{10}$ p value as measure of regression fit and effect size. I recorded the
318 number of true positive loci (TPL) among the loci beyond a predefined outlier threshold
319 (2% quantile). As GWAS performance measures, the true positive rate (TPR = recall,
320 sensitivity, discovered proportion of all QTL), positive predictive value (PPV = precision,
321 proportion of TPL among outliers considered) and false discovery rate ($1 - \text{PPV} = \text{FDR} =$
322 proportion of false positive loci among outliers considered, type I error) were calculated.
323 This was performed for all simulated scenarios.

324 *Individual GWAS (iGWAS)*

325 In addition, a traditional linear GWAS on a random sample of individuals from all
326 subpopulations was performed for all simulation scenarios (termed iGWAS hereafter). The
327 number of individuals was chosen such that the PoolSeq sequencing effort for the same
328 simulation was matched, assuming that a 15X mean coverage is appropriate for accurate
329 genotyping. A linear regression of the individuals' genotypes at each locus as predictors for
330 the phenotypes of each individual in the sample was calculated. The resulting $-\log_{10}p$
331 values were treated in the same way as described for popGWAS above.

332 Genomic prediction and validation

333 The loci identified by popGWAS were used to devise a statistical genomic prediction
334 model to obtain a score that uses observed allele frequencies at the identified loci to predict
335 the mean population phenotype of unmeasured populations. To remove remaining
336 uninformative or redundant loci, I applied feature selection, which is particularly suitable
337 for bioinformatic data sets that contain many features but comparatively few data points.
338 The minimum entropy feature selection (MEFS) technique uses mutual information to
339 measure the dependence between each feature and the target variable. For a given number
340 of features (k), the data set of the allele frequencies at selected outlier loci and the
341 respective phenotypic population means was repeatedly randomly divided in training
342 (80%) and test set (20%), a multiple regression model fitted and the r^2 -fit of the test sets to
343 the predicted phenotypes recorded. The best model for the current k was recorded and the
344 process repeated for all k in a range between 2 and the number of selected loci $- 1$. Finally,
345 the best model (i.e. highest r^2) among all k was chosen as best prediction model. MEFS was
346 implemented with the Python module scikit-learn 1.3.2 (Pedregosa et al., 2011)

347 The performance of the selected best prediction model for each run was tested with
348 independent data. Ten additional subpopulations were created and evolved under the same
349 parameters as part of the metapopulation of the initial set of populations and their mean
350 population phenotypes calculated as described above. Then the allele frequencies at the
351 predictive loci as identified by the best prediction model were extracted and phenotypic

352 prediction scores according to the best prediction model calculated. The performance of the
353 statistical genomic prediction was then evaluated by calculating the Pearson correlation
354 coefficient r between the observed mean population phenotypes and the phenotypic
355 prediction scores for the ten validation populations (Supplemental Script 2).

356 Genomic prediction and validation were performed in the same manner for iGWAS. Here
357 it was the goal to predict the individual phenotypes of a sample not used to train the model
358 with the genotypes of the loci identified by iGWAS as predictors.

359 Method performance with realistic genome sizes

360 Whether and which proportion of TPL, i.e. causal loci can be expected to be reliably
361 identified with the proposed method depends crucially on the total number of loci screened
362 as this number determines the length and size of the distributional tail of random
363 associations of neutral loci with the mean population phenotypes. The number of effectively
364 independently evolving loci in a population depends on genome size, effective population
365 size (including all factors that affect it locally and globally) and recombination rate
366 (Chakraborty, 1981; Taylor & Higgs, 2000). There are hardly any empirical estimates in the
367 literature, but dividing typical genome sizes by typical mean genome-wide LD ranges
368 suggested that a few tens of thousands to a few hundreds of thousands of independent loci
369 per genome is a realistic range for a large number of taxa (see Supplemental Table 1). I have
370 therefore considered 1,000, 5,000, 10,000, 30,000, 50,000 and 100,000 independent neutral
371 loci for samples of 12, 24, 36, 48 and 60 populations with a restricted set of parameters
372 (number of QTL and allelic contribution). As the true number of QTL underlying a trait is
373 rarely *a priori* known, I considered 10, 30, 50, 70 and 110 QTL loci in this analysis. I
374 therefore recorded the number of TPL found in sets of loci with the absolutely highest 10,
375 30, 50 and 100 $-\log_{10}p$ values, as well as outlier proportions of 0.0001, 0.001, 0.01, 0.02,
376 0.05 and 0.1 of the total number of loci in the respective simulation. As above, all
377 simulations were run in all possible parameter combinations with five replicates each
378 (Supplemental Script 3).

379 I analysed the performance of the method in an Area Under the Curve – Receiver
380 Operator Curve (AUC-ROC) and – Precision, Recall (AUC-PR) framework as suggested by
381 Lotterhos et al. (Lotterhos et al., 2022). For each combination of effective genome size and
382 number of population scored, mean TPR, PPV and FDR were calculated over all replicates
383 and parameter combinations for the respective set of simulations. The maximum F1 score
384 (Rijsbergen, 1979), the harmonic mean of the precision and recall representing both in one
385 metric, was used in addition to identify the optimal number of outliers to select.

386 All simulations were implemented in Python 3.11.7 (Van Rossum & Drake, 2009) and run
387 under pypy 3.10 (Team, 2019), the respective scripts can be found in the Supplementary
388 Material (Scripts 1-3). General statistical tests were performed with R (R Core Team, 2013).

389 Results

390 Allele frequencies at QTL loci co-vary positively with the population trait mean

391 The mean correlation coefficient between all QTL and the respective phenotypic
392 population means was positive in every parameter combination and in every single
393 simulation (Table 3).

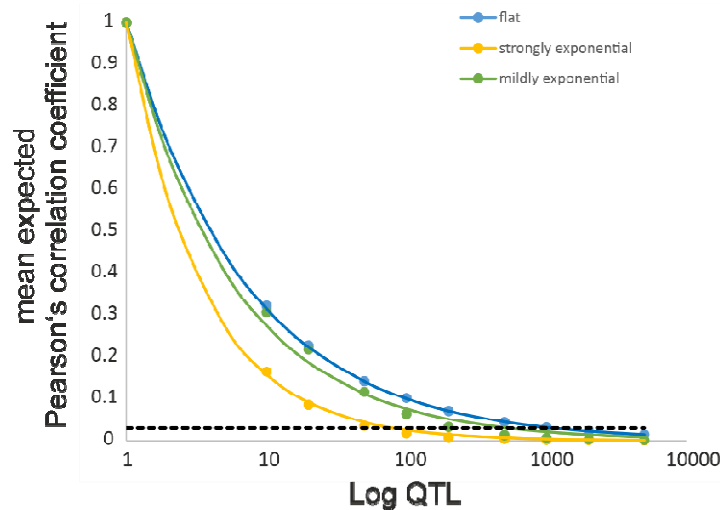
394 Table 3. Expected mean Pearson's correlation coefficients between QTL AF and
 395 phenotypic population means for three different locus contribution distributions and
 396 varying number of QTL.

n_QTL	Flat	Mildly exponential	Strongly exponential
1	1	1	1
10	0.322	0.307	0.165
20	0.227	0.218	0.085
50	0.142	0.116	0.035
100	0.101	0.064	0.017
200	0.070	0.033	0.008
500	0.045	0.013	0.003
1000	0.031	0.006	0.001
2000	0.023	0.003	0.001
5000	0.014	0.001	0.000

397

398 The expected mean correlation coefficient decreased with increasing number of
 399 contributing QTL (Figure 1). This decay was best described by a negative exponential
 400 function of the form $number\ of\ QTL^{-1/x}$ with x ranging from 1.26 in case of the strongly
 401 unbalanced locus contributions to 2 for the flat distribution.

402 Figure 1. Plot of the expected correlation coefficient between individual QTL loci and
 403 the population trait mean in dependence of the number of QTL loci. The dashed black
 404 line gives the upper 95% confidence interval for non-contributing, neutral loci.



405

406 The distribution of the correlation coefficients did not deviate from a normal
 407 distribution for the flat locus contribution distribution, while it did for all other parameters.
 408 The correlation coefficients for the non-contributing loci had an expectation of zero and a
 409 mean standard deviation of 0.01, regardless of the number of loci.

410 Influence of simulation parameters on parameters of the simulated populations

411 In an initial set of simulations, the effect of the number of generations simulated and the
 412 number of migrants on the degree of adaptation and population structure was simulated. It
 413 turned out that selection/drift equilibrium was reached after less than 10 generations. As
 414 expected, more gene-flow led to less perfect local adaptation (Supplementary Figure 3A).
 415 The time to reach the equilibrium F_{ST} among subpopulations strongly depended on the level
 416 of gene-flow. While it was swiftly reached within 50 generations for 20 or more migrants
 417 per generation, it would have taken much longer for less gene-flow (Supplementary Figure

418 3B). However, popGWAS performance was governed by the F_{ST} at the time of analysis and
419 not by selection-migration-drift equilibrium (Supplemental Figure 3C). To keep
420 computation times for the individual based model within reasonable bounds, all following
421 simulations were run for 30 generations.

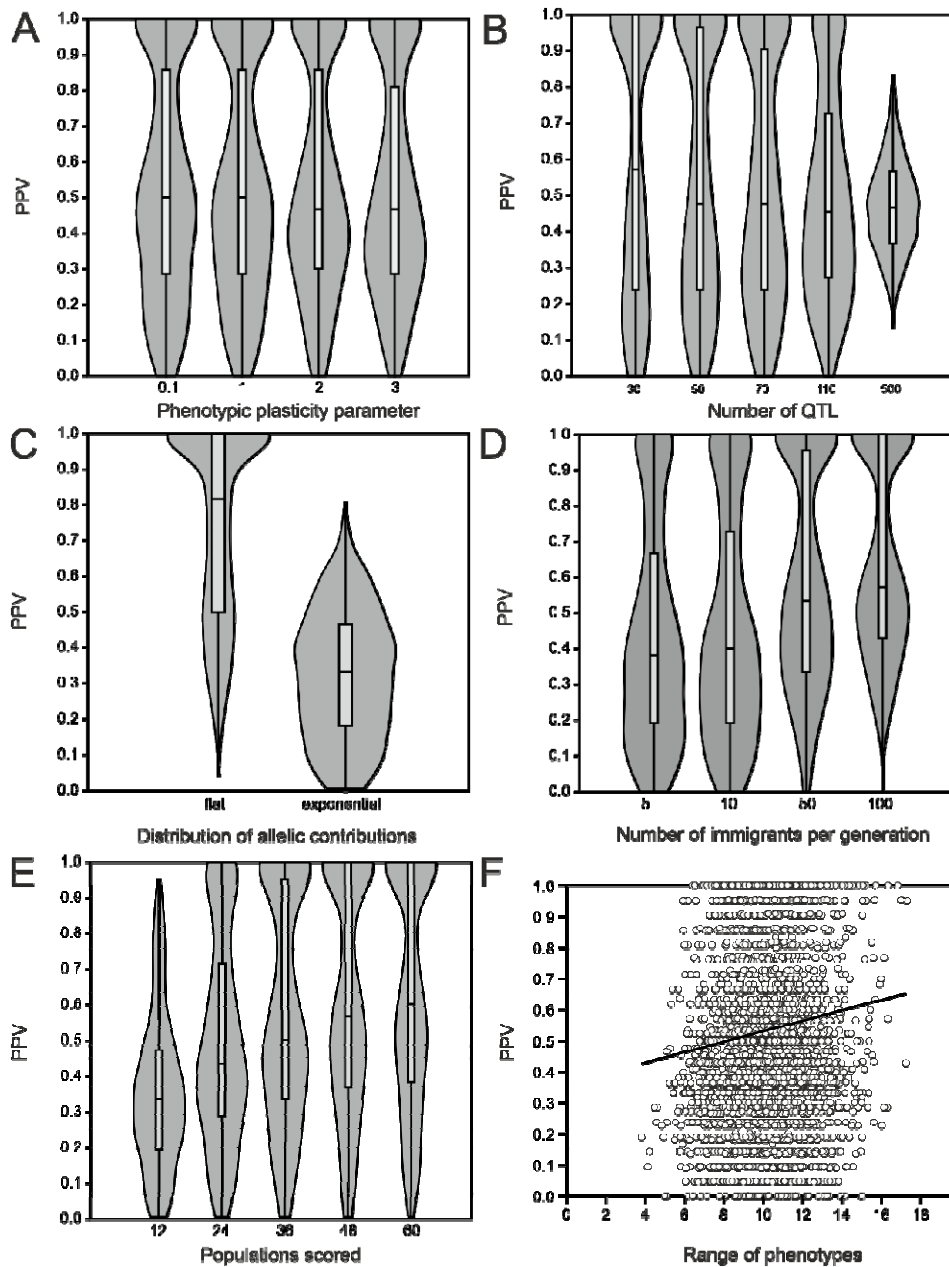
422 In the second set of simulations with 1000 neutral loci and an outlier threshold of the
423 most extreme 2% $-\log_{10}p$ values, the permutation of all parameters with five replicates
424 yielded 3884 completed independent simulation runs. The 116 missing simulations to the
425 expected 4000 runs were due to one or more subpopulations going extinct during the
426 simulation.

427 The number of migrants strongly influenced the population structure ($r^2 = 0.990$). F_{ST}
428 estimates decreased exponentially (Supplemental Figure 4A). Heritability of the trait
429 depended strongly on the environmental variation parameter ($r^2 = 0.788$, Supplemental
430 Figure 4B). It decreased on average by 0.18 per unit standard deviation, with variations of
431 up to 0.05 even among runs with identical parameters. Trait heritability estimates ranged
432 from 0.21 to 1.02.

433 Factors influencing the proportion of detected true positive loci among outliers

434 Over all simulations in the first set of scenarios, on average about 12.1 (mean proportion
435 0.52) true positive loci (TPL) were among the highest 2% outliers. The TPL values ranged
436 between none (0) and 23 (1.0); the 25 percentile was 6 (0.28), the 75 percentile 19 (0.81).
437 This exceeded in >90% of cases random expectations, when excluding the highly polygenic
438 case ($n_{qtl} = 500$), this proportion rose to more than 93%. No p-value inflation was
439 observed; the mean slope of qq-plots was 1.27 (s.d. 0.23), the distribution ranged between
440 1 and 1.99 (Supplemental Figure 4A). Supplemental Figure 5 illustrates exemplarily the
441 results of three individual simulation runs with different parameter sets.

442 Figure 2. Effect of simulation parameters and emergent features on the proportion of
443 identified true positive loci. A) ~~Phenotypic plasticity~~ **Environmental variance** parameter as a proxy for
444 heritability. B) Number of QTL. C) Distribution of allelic contributions to phenotypic
445 trait. D) Number of reproducing immigrants per generation. E) Number of
446 populations scored for population phenotypic means and allele frequencies. F) Range
447 of population phenotypic means as an emergent feature.



448

449 The environmental variability parameter had no significant effect on PPV ($F = 0.13$, $p =$
 450 0.939 , Figure 2A). The number of QTL showed a systematic effect on mean PPV (ANOVA $F =$
 451 19.4 , $p = 1.32 \times 10^{-15}$, Figure 2B). The distribution of allelic effects on the trait showed a
 452 huge effect on the mean PPV (mean equal contribution = 0.81 , mean exponential = 0.32 , $F =$
 453 3409 $p = 0$, Figure 2C). The relation of mean proportion of detected TPL and number of
 454 migrants was approximately linear. The more migrants per generation, the higher the
 455 probability to detect more contributing loci. This effect was strong ($F = 112$, $p = 2.35 \times 10^{-}$
 456 70) were observed. The number of populations screened had a similarly strong effect on
 457 proportion of TPL among the selected loci ($F = 117.4$ $p = 4.70 \times 10^{-95}$). The values ranged
 458 from a mean PPV of 0.35 (s.d. = 0.21) with 12 populations to over 0.63 (s.d. = 0.32) with 60
 459 populations. Given the chosen threshold, a diminishing return was observed above 36
 460 populations sampled (Figure 2E). The phenotypic range in a simulation run had a low ($r =$

461 0.11, $p = 3.02 \times 10^{-11}$), yet significantly positive effect on detection of TPL. The realised
462 range of population trait means in the simulations covered on average 16% (range = 0.1-
463 57%) of the possible range. An increase of one unit in range increased the proportion of
464 TPL by 0.02 (Figure 2F).

465 When jointly considering the effect of all parameters on PPV in a GLM, it turned out that
466 all had a significant effect (Table 4). Their relative influence increased from phenotypic
467 range ($r^2 = 0.03$) over heritability ($r^2 = 0.06$), number of QTL ($r^2 = 0.07$), F_{ST} ($r^2 = 0.19$),
468 number of populations ($r^2 = 0.20$) to the number of allelic contributions, that had by far the
469 greatest influence ($r^2 = 0.45$). In total, the parameters explained 66.4% of variance.

470 Table 4. Generalised Linear Model of factors influencing the proportion of TPL among
471 outliers (PPV) in simulations.

Factor	Coefficient	Std.err.	t	p	r^2
Constant	0.33	0.02	18.00	<2e-16	
range_pheno	0.01	0.00	4.02	0.00006	0.03
heritability	-0.14	0.01	-10.10	<2e-16	0.06
n_qtl	0.00	0.00	-10.63	<2e-16	0.07
F_{ST}	-5.72	0.19	-29.84	<2e-16	0.19
n_pop	0.01	0.00	28.47	<2e-16	0.20
allelic_contr	0.43	0.01	73.35	<2e-16	0.45

472

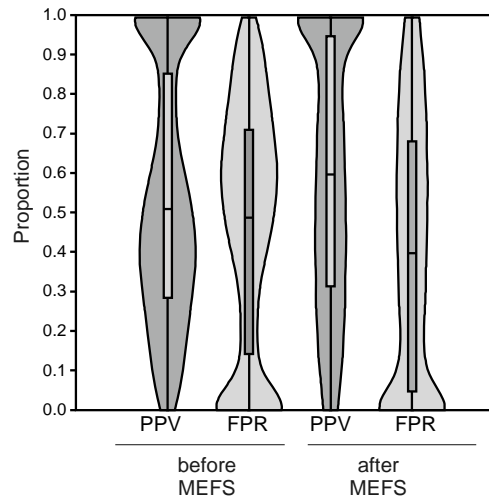
473 Hierarchical population structure

474 The introduction of a hierarchical population structure in simulations with a restricted
475 parameter set did not change much with regard to the relative influence of the parameters
476 (Supplemental Figure 6 A-F). The initial divergence parameter had no effect on PPV. The
477 number of QTL loci ($F = 12.13$, $p = 7.38 \times 10^{-6}$), the distribution of allelic contribution ($F =$
478 888 , $p = 7.73 \times 10^{-109}$) and the number migrants per generation ($F = 18.7$, $p = 1.88 \times 10^{-5}$)
479 had a significant effect, just like the number of regions, going along with a growing number
480 of subpopulations ($F = 4.06$, $p = 0.02$). The final overall F_{ST} had a significant influence ($p =$
481 2.1×10^{-5}), albeit with a relatively low effect size ($r = -0.20$).

482 Minimum Entropy Feature Selection and statistical phenotype prediction

483 Minimum Entropy Feature Selection (MEFS) removed on average 8.72 (range = 2-14,
484 s.d. = 4.14) loci, corresponding to a proportion of 0.38 (s.d. = 0.19) from the initially chosen
485 outlier set. The procedure removed on average a larger proportion of FP than TPL (mean
486 difference 0.14, $t = -19.9$, $p = 6.7 \times 10^{-79}$). This increased the proportion of TPL in the final
487 prediction set on average by 0.05 (range = -0.23-0.48, s.d. = 0.09) to a mean of 0.66 (range
488 = 0-1, s.d. = 0.29, Figure 3).

489 Figure 3. Effect of Minimum Entropy Feature Selection (MEFS) on the proportion of
490 TPL and FP in the selected set.

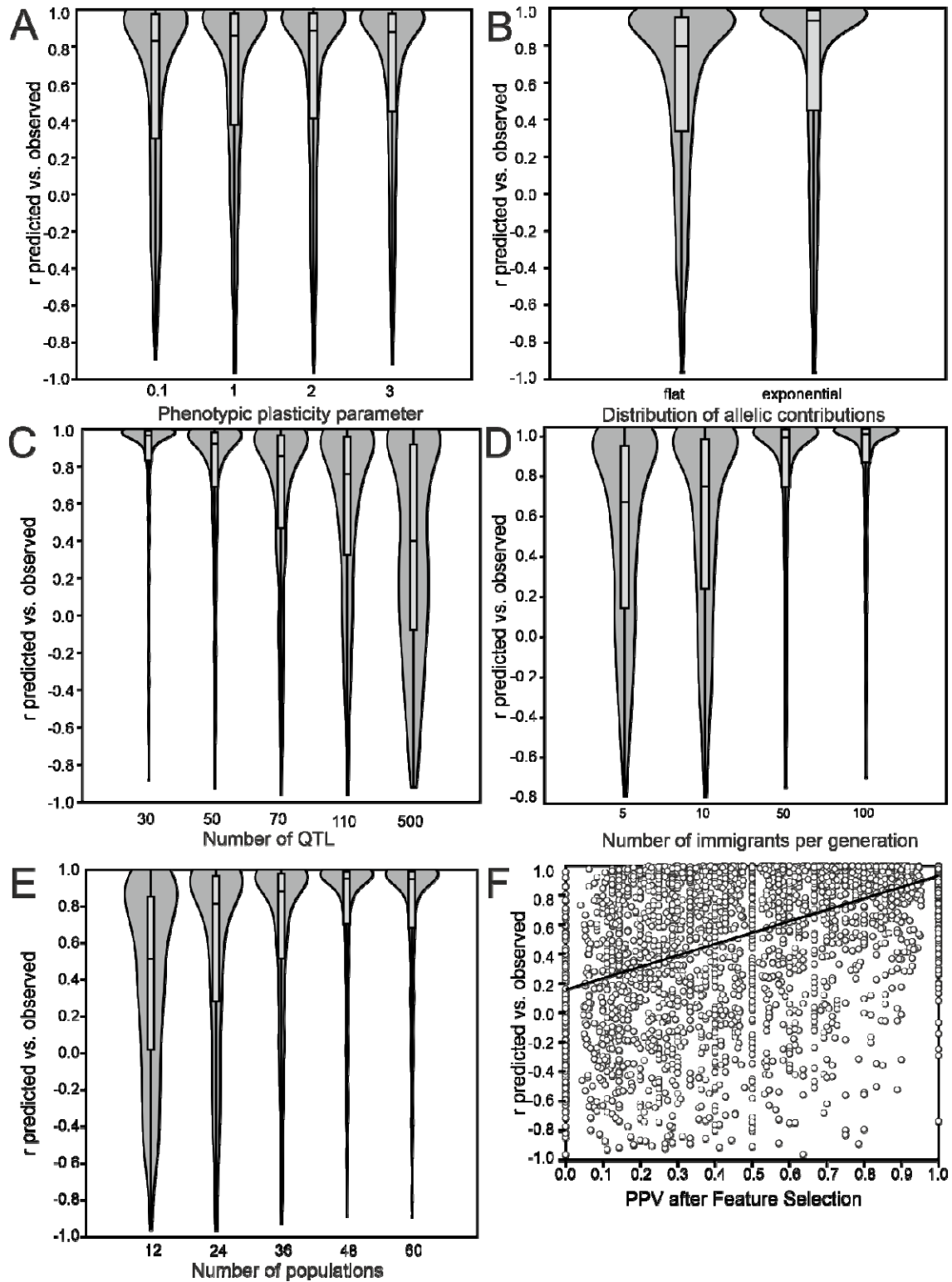


491

492 The predictive accuracy of the SNP loci sets selected by MEFS was on average $r = 0.61$
493 (s.d. = 0.48). It ranged from -0.96 to 1.0. The distribution was highly skewed with 75%
494 being higher than 0.37, the median was found at 0.86 and still 25% being higher than 0.97
495 (Supplemental Figure 4B).

496 The accuracy of mean population phenotype prediction depended linearly on the
497 number of TPL in the prediction set ($r^2 = 0.28$, $p = 0$), with any additional TPL increasing
498 the correlation coefficient by 0.05. Inversely, the accuracy of prediction decreased with a
499 rising number of FP, but even with a considerable number of FP in the prediction set,
500 accurate prediction was possible in a large number of cases. Overall, the prediction
501 accuracy increased with increasing proportions of TPL among the prediction set, although
502 even 100% TPL in the prediction set did not guarantee a highly accurate prediction ($r >$
503 0.8) in all cases.

504 Figure 4. Influence of simulation parameters on the accuracy of statistical population
505 mean phenotype prediction. A) Phenotypic plasticity parameter as proxy for
506 heritability. B) Distribution of allelic trait contributions. C) Number of trait-
507 underlying QTLs. D) Generation of independent evolution as proxy for population
508 structure. E) Number of populations scored. F) Proportion of TPL in the prediction
509 loci set after MEFS.



510

511 As the prediction accuracy depended on the proportion of selected TPL, their relation to
512 the individual simulation parameters was very similar to the results described in the
513 previous section, except for the distribution of allelic contributions where the prediction
514 accuracy was better for loci with exponential effects (Figure 4A-F). The number of
515 populations screened was the most important factor. With 36 or more populations

516 screened, 97.8% of simulations showed a prediction accuracy of 0.8 or better, independent
517 of the other simulation parameters applied. In a GLM with all factors simultaneously
518 considered, the proportion of TPL selected had the largest influence on prediction accuracy
519 ($r^2 = 0.28$), followed by F_{ST} (0.19), the number of QTL (0.18), distribution of allelic
520 contributions (0.17), the number of populations screened (0.11). Heritability had only a
521 minor influence on the prediction accuracy (0.06), while the range of phenotypes was not
522 relevant (Table 5).

523 Table 5. Generalised Linear Model of factors influencing the accuracy of statistical
524 phenotypic population mean prediction.

Factor	Coefficient	Std.err.	t	p	r^2
Constant	0.69	0.04	17.31	<2e-16	
range_pheno	0.01	0.00	1.61	0.109	0.02
heritability	-0.16	0.03	-5.65	1.77E-08	0.06
n_pop	0.00	0.00	10.05	<2e-16	0.11
allelic_contr	-0.21	0.01	-15.93	<2e-16	0.17
n_qtl	0.00	0.00	-18.62	<2e-16	0.18
F_{ST}	-7.63	0.42	-18.04	<2e-16	0.19
PPV after MEFS	0.51	0.02	24.50	<2e-16	0.28

525

526 Performance comparison to individual GWAS

527 In every single simulation, iGWAS performed worse than popGWAS. The approach based
528 on individuals found on average 7.42 TPLs (PPV 0.31), compared to 12.15 (PPV 0.53) with
529 popGWAS (Suppl. Figure). This difference in means of 4.73 loci was highly significant in a
530 pairwise t-test ($t > 3000$, $p = 0$). The results for hierarchically structured population were
531 similar (mean difference 5.7 loci, paired t-test $t = 19.62$, $p = 1.6 \times 10^{-62}$). In more than 70%
532 of simulations, it was not possible to calculate a valid phenotypic prediction model for
533 individuals with the identified loci. For the remaining cases, the mean predictive accuracy
534 for the individual's phenotype was 0.079.

535 Method performance with realistic effective genome sizes

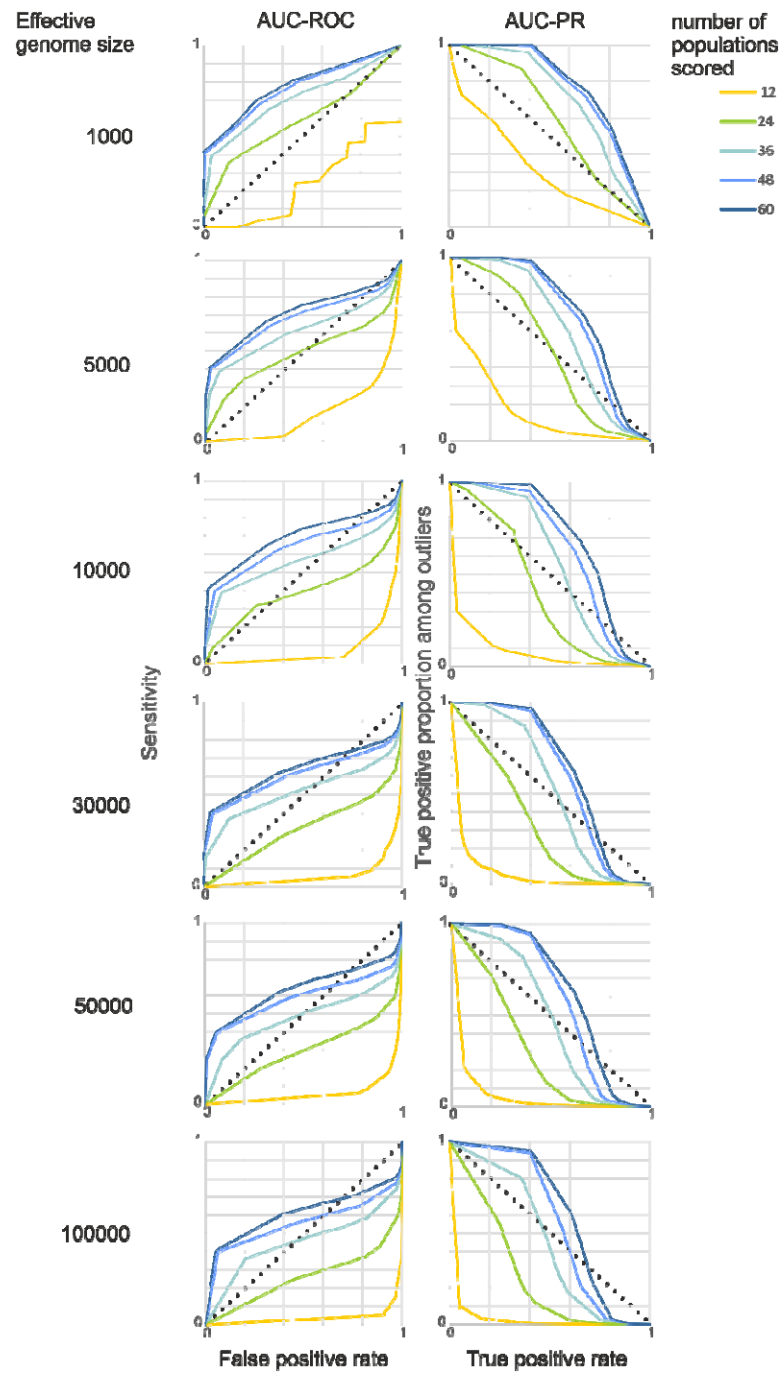
536 The values for AUC-ROC ranged between 0.067 and 0.833, for AUC-PR between 0.013
537 and 0.730. There was an interaction between the effective genome size and number of
538 populations scored. According to both AUC measures, the method performed best, when the
539 number of populations scored was high and the genome small (Figure 5). An at least
540 satisfactory (> 0.66 for AUC-ROC and > 0.53 for AUC-PR) overall performance was
541 observed for 24 populations for the smallest genomes considered (1,000), for 36
542 populations up to 30,000 independent loci and for genome sizes up to 100,000 for 48 and
543 60. The similar values in both statistics and the plots suggested that there are diminishing
544 returns for samples larger than about 48 populations. Moreover, closer inspection of the
545 corresponding plots (Figure 6) suggested that for samples of 48 and 60 populations, an
546 optimal ratio between TPL and FPL exists for approximately the 25 highest outlier loci,
547 independent of genome size. For combinations with good performance, the maximum F1
548 score suggested that choosing the 30 highest outlier provided the optimal compromise
549 between maximising TPR and minimising FPR (Supplemental Figure 7).

550 Figure 5. Heat-map of AUC-ROC (area under the curve - receiver operator
551 characteristics) and AUC-PR (area under the curve - precision recall) in relation to
552 effective genome size and number of populations scored.

AUC-ROC		number of populations scored					AUC-PR		number of populations scored				
effective genome size		12	24	36	48	60	effective genome size		12	24	36	48	60
	1000	0.391	0.663	0.769	0.817	0.833		1000	0.250	0.514	0.644	0.709	0.730
5000	0.198	0.430	0.677	0.746	0.776	5000	0.125	0.430	0.552	0.623	0.654		
10000	0.112	0.459	0.623	0.700	0.754	10000	0.060	0.338	0.508	0.587	0.644		
30000	0.094	0.375	0.668	0.668	0.697	30000	0.038	0.265	0.464	0.553	0.582		
50000	0.096	0.359	0.539	0.644	0.696	50000	0.032	0.238	0.422	0.532	0.577		
100000	0.067	0.339	0.528	0.616	0.670	100000	0.013	0.182	0.378	0.497	0.551		

553

554 Figure 6. AUC-ROC and AUC-PR for a range of effective genome sizes. In the left
555 column are the plots of AUC-ROC, i.e. FDR on the x-axis versus TPR on the y-axis. The
556 right column shows AUC-PR plots, i.e. TPR on the x-axis versus PPV on the y-axis. The
557 dotted lines indicate the threshold for a random effect.



558

559

560

Discussion

561 This study used extensive forward simulations to explore the potential of a novel GWAS
562 approach utilising phenotypic population means and genome-wide allele-frequency data to
563 identify loci potentially underlying the population differences in quantitative polygenic
564 traits and predict the mean phenotypes of unmeasured populations. While the approach
565 seems to be generally useful in a wide range of cases, there are also clear limits to its
566 applicability.

567 General validity of the underlying assumptions

568 The first major goal of the study was understanding the conditions under which the
569 hypothesised pattern of a linear relation between the population allele frequencies at causal
570 loci and the phenotypic population means of the respective trait emerges. The initial
571 simulations demonstrated that the expectation for the covariance of random population
572 "allele frequencies" at contributing quantitative trait loci (QTL) and the respective
573 population trait mean is consistently positive when an additive model applies. This is an
574 inherent consequence of the common dependence of both variables on the QTL genotypes
575 of the individuals in a population, as demonstrated in (3). Additive models seem to be an
576 appropriate statistical approximation for most quantitative traits at population level (Hill et
577 al., 2008), despite the description of many epistatic interactions on the molecular level
578 (Moore & Williams, 2005).

579 The relation appeared to be largely independent of the distribution shape of locus
580 contributions to the trait. While in the case of equal contributions i.e. a flat distribution, the
581 correlation coefficients of individual loci are themselves a random variate, normally
582 distributed around the expected mean. As the distribution becomes increasingly skewed,
583 locus contribution becomes predictive of the correlation to the trait. Loci contributing more
584 to the trait and thus accounting for more of the phenotypic variance will likely have a higher
585 correlation of their allele frequencies to the population mean. Conversely, the expectation
586 for non-contributing loci is approaching zero. Therefore, it is principally possible to exploit
587 the correlation between allele frequencies and population trait means for the identification
588 of loci underlying an additive quantitative trait.

589 However, some statistical limitations became obvious. Firstly, as the number of QTL
590 increases, the expected mean correlation coefficients become so small that they are likely to
591 be indistinguishable from the tail of the zero-centered normal distribution of non-
592 contributing loci, even with an unrealistically high number of samples. Consequently, the
593 method for identifying QTL by the positive covariance of their allele frequencies with the
594 population trait means is *a priori* more suited for oligogenic to moderately polygenic traits.
595 Secondly, the number of QTL and the distribution of locus contributions may influence the
596 statistical identifiability of individual QTL. In particular, loci that contribute only minimally
597 to the trait or that fall by chance below the expected mean correlation coefficient may
598 overlap with the tail of the distribution of non-contributing loci.

599 These predictions remind of similar conditions for the contribution of different QTL
600 architectures to phenotypic adaptation described by (Höllinger et al., 2023). They assert that
601 phenotypic adaptation of oligogenic traits is achieved by detectable allele frequency shifts
602 at some but not very many loci, while adaptation in highly polygenic traits is rather
603 achieved by subtle perturbations of standing variation, with respective consequences for

604 their detectability. Just as expected here, they stress the importance of stochastic effects
605 that may lead to apparently heterogeneous locus contributions (Höllinger et al., 2023).

606 Interestingly, deviation from a selection-drift-migration equilibrium were not an
607 impediment for detecting contributing loci. Best possible adaptation was regularly achieved
608 within less than 10 generations. True to theoretical expectations, higher gene-flow among
609 populations led to less perfect local adaptation for a given selective strength (Brady et al.,
610 2019). Drift-migration balance was not reached within a reasonable number of generations.
611 This was, however, not relevant for popGWAS performance, which was mainly driven by
612 the degree of population differentiation, everything else being equal. This insensitivity to
613 equilibrium conditions is an advantage of the method as natural populations tend not to be
614 in equilibrium (Müller et al., 2022). Rather, natural populations are constantly tracking
615 variable selective optima (Pfenninger & Foucault, 2022; Rudman et al., 2021), which leads
616 to intermediate allele frequencies at the loci under such a selective regime (Höllinger et al.,
617 2023).

618 Limiting factors for the identification of contributing loci in natural settings

619 The Wright-Fisher forward simulations of a quantitative trait in a subdivided population
620 with realistic properties and sample sizes largely confirmed the theoretical expectations. In
621 particular when a sufficient number of populations was scored (in this case more than 36),
622 a large proportion of true positive loci could be reliably identified, with the exception of a
623 few parameter combinations. The genetic architecture of the trait was an important
624 predictor for the ability to identify causal loci. While loci underlying oligogenic and
625 moderately polygenic traits could be fairly reliably identified, the highly polygenic scenario
626 tested (500 loci) performed poorly. A higher proportion of TPL was identified when the
627 locus contribution to the trait was identical than in the case of an exponential trait
628 contribution distribution. This was likely due to the tendency of higher correlations
629 between higher contributing loci and the trait, which allowed the loci from the tail of the
630 distribution to vary freely, making them indistinguishable from non-contributing loci.

clarify: exponential dis

631 The influence of mean heritability was on GWAS performance was not marked. Even
632 down to trait heritability estimates of 0.3, the success rate was only slightly reduced. This
633 effect may be attributed to the averaging of phenotypes and genotypes across multiple
634 individuals, which is likely to mitigate the inherent noise associated with individual data
635 (Johri et al., 2022; Stinchcombe & Hoekstra, 2008). This finding is consistent with
636 observations by (Zhang et al., 2018), who employed pooled data for GWAS. From a practical
637 standpoint, the findings suggest that inevitable errors in phenotyping, which can
638 compromise GWAS performance on individuals (Barendse, 2011), are likely to be less
639 problematic when using the mean measured over many individuals. Furthermore, this
640 finding indicates that the failure to entirely remove non-additive variance from the analysis
641 does not necessarily compromise the method's ability to reliably identify trait-associated
642 loci.

643 From a statistical perspective, it was anticipated that the range of phenotypic population
644 means would influence the identification of true positive loci to some extent, given that a
645 larger range of phenotypic means is inherently associated with on average larger allele-
646 frequency differences among populations. The choice of populations with a large range of
647 environmentally unexplained variance is therefore crucial. It is, however, important to
648 emphasise that the underlying causes of the observed differences in trait means among
649 populations are not of primary concern. These may be attributed to local adaptation, but

unclear why it should be

650 also to maladaptation, human choice, or other factors. Likewise, increasing the number of
651 populations screened increased the statistical power of the approach. However, it seemed
652 that increasing the number of samples led beyond a certain threshold to diminishing
653 returns in statistical power gain.

654 Effect of population structure on the detection of contributing loci

655 It is long-since known that population structure can have a confounding effect on GWAS
656 studies (Marchini et al., 2004). Confounding associations between ~~two-allelic SNPs~~ and a
657 phenotype may easily arise in iGWAS, because phenotypically more similar individuals may
658 be also genetically more similar because they share common ancestry as members of the
659 same family/population/clade. In addition, a quantitative or qualitative phenotype (y) in
660 iGWAS is related to a genotype (x) either by a linear or logistic model – with exactly three
661 possible values of x. This leads inherently to low statistical power, requiring a very high
662 number of individuals (O'Connor, 2021) and extensive corrections for population structure
663 to obtain a reliable statistical association (Sul et al., 2018). popGWAS follows a principally
664 different approach; the possible values of x are allele frequencies in different populations
665 and thus limited only by sampling effort. This gives the approach a strong inherent
666 statistical advantage, which might be also the reason that the method does not suffer from
667 p-value inflation.

668 Population structure can nevertheless interfere with reliable associations in popGWAS,
669 albeit for different reasons. A pronounced population structure ($F_{ST} > \sim 0.07$) was **a indeed**
670 **major factor** impeding reliable identification of true positive loci, even with a high number
671 of samples and regardless of the reasons for the structure. However, this was probably
672 more due to distinct evolutionary trajectories in independently evolving populations. If the
673 evolutionary trajectory of the populations analysed is sufficiently independent, either by
674 drift and/or differential availability of adaptive mutations, similar phenotypes may have a
675 differential genomic basis, allowing at best to identify any common variants. The genetic
676 redundancy of polygenic traits can lead to evolution of the same phenotypes from different
677 genomic bases (de Vladar & Barton, 2014; Kaneko & Furusawa, 2006), even if evolving from
678 the same ancestral population (Barghi et al., 2019, 2020; Pfenninger et al., 2015). If
679 different loci in different populations are causal for the observed phenotypic differences, a
680 linear relation between population means and allele frequencies is not to be expected. It is
681 therefore important that the allele frequencies in the studied populations are correlated
682 either by recent common descent and/or recurrent gene-flow, i.e. that the population
683 structure between the population scored is weak (Mathieson, 2021).

684 By relating allele frequencies with mean phenotypes false associations may also arise, if
685 the trait under scrutiny is effectively neutral and thus the constituting loci follow the overall
686 drift pattern or the ecological differences causing the phenotypic differences are associated
687 to an isolation-by-distance pattern. In this case, the matrix of mean phenotypic population
688 differences (or Q_{ST}) should show a strong positive correlation with the overall F_{ST} matrix
689 among populations. A trait showing this easily testable pattern may therefore *a priori* not
690 be suitable for analysis with the method. To avoid such a situation, it is recommended to
691 test for (the absence of) a correlation between genome-wide genetic distance and
692 differences in phenotypic means (e.g. by a Mantel's test).

indeed a major factor

693 Accurate statistical genomic prediction in a wide range of conditions

694 Genomic prediction is deemed to be one of the major tools for the mitigation of climate
695 change on biodiversity (Aguirre-Liguori et al., 2021; Bernatchez et al., 2023; Capblancq et al.,
696 2020; Waldvogel et al., 2020). One of the major findings of the presented approach was the
697 highly accurate prediction of the phenotypic population means from genomic data above a
698 certain number of populations screened. Given the limited performance of genomic
699 prediction in a medical context (Visscher et al., 2017) this was initially quite surprising.
700 However, it should be *a priori* easier to predict the differences in population means
701 compared to differences among individuals for the following reasons. The difference in
702 means among subpopulations was mostly governed by only a couple of loci, because the
703 range of phenotypic population means extended over only a relatively small part of the
704 theoretically possible range. This applies to the simulations but most likely also in nature it
705 is improbable to encounter populations that are (nearly) fixed for the respectively
706 alternative alleles over all or even most trait contributing loci and show an accordingly
707 extended phenotypic range. Consequently, already the allele frequency differences of a
708 couple of loci actually need to follow a linear model to explain most of the variance among
709 phenotypic population means – the rest is free to vary and behave (almost) like neutral loci.
710 Even the fit of the highest outlier loci to a linear model was far from perfect as was expected
711 from the genetic redundancy of a polygenic trait architecture (Barghi et al., 2020).
712 However, as long as these important loci are the same over the majority of subpopulations
713 (either due to common descent or gene-flow), accurate predictions of population trait
714 means from these loci is therefore possible. Such loci likely have an intermediate frequency,
715 because alleles of very low or very high frequency (i.e. present only in few or **almost** all
716 individuals with not necessarily extreme phenotypes) by definition cannot have a large
717 impact on the phenotypic population mean, even when of large effect. Conversely, the
718 individual phenotype can be mainly determined by rare alleles of large effects. Therefore, a
719 locus whose AF is important for the difference in means among populations might have
720 rather low predictive power for the individual, because as a locus of likely intermediate
721 frequency, all genotypes are necessarily realised with high probability within a population.
722 The accurate prediction of individual phenotypes thus likely requires much more loci than
723 the prediction of the phenotypic population mean.

argumentation hard to

724 Finally, it is crucial to distinguish between two major goals of GWAS: i) find the loci
725 functionally underlying biologically relevant variation and ii) the accurate prediction of
726 untyped instances. As (Shmueli, 2010) pointed out, the goals of explaining a phenomenon
727 on the one hand and predicting it on the other are related but not identical. In particular it is
728 important to note that an accurate prediction model does not need to contain all features
729 that are necessary for a comprehensive functional description of the system (Shmueli,
730 2010). For accurate prediction, it is not even necessary that all features in the prediction
731 model have actually a functional role, as long as they are statistically strongly associated
732 (Shmueli, 2010). While the results have shown that prediction tends to become more
733 accurate if more truly functional loci are included, it is therefore not necessary that the
734 prediction model includes all or even most of the functional loci.

735 Contrary to its application in medicine or selective breeding (Wray et al., 2019), however,
736 accurate prediction of population responses is in many instance of the current biodiversity
737 crisis probably more important than the prediction of individual phenotypes. Within the
738 limits outlined above, the proposed method delivered in many instances very accurate
739 predictions ($r > 0.8$ in $> 90\%$ of cases for more than 36 populations) of population mean

740 phenotypes. It should be noted, however, that the prediction is statistical in the sense that it
741 produces a prediction score (de Los Campos et al., 2018) that correlates with the mean
742 population phenotype and is explicitly not a comprehensive functional quantitative genetic
743 model of the trait. Just like with any other genomic prediction (Kachuri et al., 2024), this
744 limits the transferability of the prediction to other, more distantly related lineages or
745 species.

746 Reducing the false positive rate before prediction is in any case advisable, as it proved to
747 be the most important factor of prediction success with independent data. The application
748 of a Machine learning approach, in this case Minimum Entropy Feature Selection (MEFS),
749 prior to prediction effectively reduced the already low false positive rate among the initially
750 selected loci further. Whether other approaches would yield even better results remains to
751 be tested. Other population genetic parameters influenced prediction success in a very
752 similar fashion as the initial true positive rate. One notable exception was distribution of
753 locus contributions. While true positive loci were more reliably identified from a flat
754 distribution, prediction worked better when many loci of large effect were among the
755 prediction set, most likely because these loci contribute more to phenotypic variance
756 among populations (Jain & Stephan, 2015).

757 Typical genome sizes of real species are no obstacle

758 The perhaps most important challenge was showing that the proposed method has
759 enough statistical power to distinguish at least a part of the unknown, but likely relatively
760 small number of QTL reliably from the large number of non-contributing loci in real
761 genomes of real species. The evaluation of method performance with AUC-ROC and AUC-PR,
762 as recommended recently (Lotterhos et al., 2022), showed a satisfactory performance even
763 for genomes with moderately high effective sizes, provided a sufficiently high number of
764 populations is screened. In particular restricting the selection of potentially causal QTL on a
765 few dozen of the highest outliers promises to yield very low false positive rates. However,
766 as the success rate depended very much on the biological characteristics like genome size,
767 population structure, LD and so on, of the investigated taxon, no general recommendations
768 can be given here, except to carefully take them into account. As shown above, already a
769 limited number of true positive loci may be sufficient for reliable genomic prediction.

770 Practical considerations

771 The proposed method finds rather genomic regions or haplotypes associated to the trait
772 in question than directly causal SNPs. However, this is true for most GWAS methods (Wang
773 et al., 2010) and therefore fine-mapping and inference of causal processes remain to be
774 done (Wallace, 2021). In practice, this requires that regions with high SNP outlier density
775 need to be collapsed to haplotypes prior to further analysis. Knowledge on the local LD-
776 structure, mean haplotype length, respectively recombination landscape can aid haplotype
777 identification (Flister et al., 2013). Recently developed machine learning approaches makes
778 such information available for pooled data (Adrion et al., 2020).

779 The possibly largest advantage of the proposed method is therefore its data efficiency, if
780 pooled sequencing is applied. Because the Pool-Seq approach (Schlötterer et al., 2014) yields
781 highly accurate estimates of genome-wide allele frequencies at SNP sites (Czech, Peng,
782 Spence, Lang, Bellagio, Hildebrandt, Fritschi, Schwab, Rowan, & consortium, 2022) the
783 necessary sequencing effort is marginal compared to individual based approaches
784 (Ziyatdinov et al., 2021). This is mainly due to the relatively reduced costs for library

785 preparations necessary that, depending on the genome size, often make up a large share of
786 or even exceed the actual sequencing costs in individual analysis. Moreover, the popGWAS
787 method out-performed iGWAS in all cases, if the same sequencing effort is applied as a
788 benchmark.

789 The proposed method makes GWAS studies accessible for the usual funding in the field
790 of biodiversity. Pooled sequencing for GWAS has been proposed (Yang et al., 2015) and
791 applied (Giorello et al., 2023; Kumar et al., 2022; Pfenninger et al., 2021) with extreme
792 phenotypes. Automated large scale phenotyping is a very active field of research, with
793 satellite or other remote sensing approaches, flow cytometry, bulk measurements of
794 metabolic rates, metabolomes, transcriptomes, pooled HPLC or mass spectrometry,
795 automated video-based phenotyping, mass CT scanning provides already access to large
796 amounts of data. Sampling the required number of demes or subpopulations can pose a
797 challenge for certain taxa, however, e.g. biodiversity monitoring schemes or museum
798 collections may offer readily access to respective samples. Application of the method to a
799 real world data set from European beech on phenological traits (Pfenninger et al. in prep),
800 showed that such an approach can be successfully performed with moderate logistic effort.
801 Many of the identified loci by popGWAS were previously implicated in phenological traits
802 and yielded excellent predictive power in predicting the mean phenotypes of independent
803 populations (Pfenninger et al. in prep).

804 **Conclusion**

805 This study demonstrated the potential of the proposed GWAS approach for biodiversity
806 genomics. As with any GWAS method, its usefulness depends on the study goals. If it is the
807 aim to infer all loci in a genome contributing to a given quantitative trait and to quantify
808 their relative influence, probably no existing (single) GWAS method and no experimental
809 design can achieve this. If it is the goal to accurately predict individual quantitative
810 phenotypes with the inferred genomic basis, e.g. for medical or breeding purposes, the
811 suggested method may not lead very far, as detailed above. Nevertheless, it can add a
812 substantial number of candidate loci that are not easily found by other methods. However, if
813 it is important **to** to infer the major contributing loci for quantitative differences in
814 ecologically relevant traits observed among natural populations, popGWAS can be a
815 valuable tool. By carefully considering the factors influencing its performance and
816 addressing the limitations, this method holds some promise in identifying the genetic basis
817 of complex traits and performing accurate statistical predictions of phenotypic population
818 means from genomic data in natural populations.

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Conflict of interest disclosure

825 The author declares that he complies with the PCI rule of having no financial conflicts of
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827

Data, scripts, code, and supplementary information availability

828 Supplementary information including the Python code used for the simulations is
829 available at <https://10.5281/zenodo.11562472>

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